SMEFT projections at the EIC and LHeC to NLO QCD

Candidacy Talk

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- sections at the LHeC.
- BSM effects are parametrized in the model-independent SMEFT framework.
- coefficients introduced as effective couplings at a UV scale Λ :

$$\mathscr{L}_{\text{SMEFT}} = \mathscr{L}_{\text{SM}} + \sum_{n>4} \frac{1}{\Lambda^{n-4}} \sum_{k} C_k^{(n)} O_k^{(n)}$$

- accessible collider energy.
- fermion operators at n = 6.

• We study PVDIS asymmetries in NC cross sections at the EIC and NC DIS cross

• Higher-dimensional operators are built using the existing SM particles with Wilson

• All new physics is assumed to be heavier than all the SM states and well beyond

• We focus on SMEFT corrections to the ffV vertices, as well as semi-leptonic 4-

We find that

- the EIC can probe complementarily and competitively to the LHC NC Drell-Yan, resolving blind spots observed;
- the EIC can barely compete with the LHeC; nonetheless, they yield distinct correlations, showing complementarity;
- flat directions observed in the fit one LHeC run can be resolved by other runs and even by the EIC; and
- the LHeC seems promising in resolving flat directions in the ffV sector observed in the EW pole-observable (EWPO) fits.





EIC and LHeC

Next-gen electron-hadron colliders: EIC and LHeC

Electron-hadron colliders: [Brüning *et al.* FPhy (2022)]

- Ultimate tool for high-precision QCD studies
- Ultimate microscope for probing internal structure of hadrons
- e^- is an ideal probe of proton structure due to unmatched precision of QED interaction:
 - Virtual photon and vector bosons probe proton structure in a clean environment
 - Kinematics is uniquely determined by e^- beam and scattered lepton
- Hadron-Elektron-Ringanlage (HERA @ DESY, Germany) was the only e^-H collider ever operated (1991-2007).
- Electron-Ion Collider (EIC) is currently under construction at BNL @ NY.
- Large Hadron-electron Collider (LHeC @ CERN, Switzerland) is awaiting approval.

- A US DOE project under construction in Brookhaven National Laboratory, Upton, NY.
- It will use the Relativistic Heavy Ion Collider (RHIC @ BNL, in operation since 2000) accelerator complex. (RHIC is the first heavy-ion collider and also the world's only spinpolarized proton collider.)
- It will combine the experience from HERA to deliver polarized e^- beams with the experience from RHIC to be the first machine that provides the collision of polarized e^{-1} with polarized p, and at a later stage, polarized 2 H and 3 He.
- It is planned to start operating in a decade.

Image credit: bnl.gov



HC [Accardi *et al.* 1212.1701]

Unique features:

- ion beams up to 110 GeV.
- First lepton-ion collider to polarize both beams
- First collider with fast spin-flip capacity

• Designed to collide 5 to 18 GeV polarized e⁻ beams with 41 to 275 GeV polarized p beams, polarized light ions with energies up to 166 GeV (³He), and unpolarized heavy

• CM energies between fixed-target scattering and high-energy colliders, 70 to140 GeV



EIC [Accardi *et al.* 1212.1701]

From these unique features:

- Extraction of PVDIS asymmetries in EW NC cross section
- Reduced uncertainties from luminosity and detector acceptance/efficiency
- Explore issues in QCD
- Probes of BSM physics

Also a positron beam in the future to study electron-positron (lepton-charge) asymmetries.

[Fernandez et al. 1206.2913]

- approved).
- Center of mass energies of $\sqrt{s} \simeq 1.5$ TeV for DIS measurements:
 - Searches and analysis for BSM physics
 - Novel measurements in QCD
 - EW physics to unprecedented precision
 - DIS physics at low Bjorken x
- Suggested electron beam energies: 50 to 150 GeV; the chosen default value is 60 GeV.

• 1984: Idea of an e^-p collider in the LEP-LHC tunnel was first discussed (around the same time HERA was

• 2005: It was found feasible to simultaneously operate pp in the LHC and ep in the new machine termed LHeC, which would be complementary to the LHC (just as HERA was to Tevatron). Integrated luminosity was projected to be O(100) fb⁻¹, a factor of 100 more than HERA had collected over its lifetime of 15 years.



W. Kandinsky, Circles in a circle. Image credit: wassilykandinsky.net

[Fernandez et al. 1206.2913]

- 2011: First complete draft of conceptual design of the LHeC • The LHeC will be an upgrade of the LHC.
- - Substantially enriches the physics harvest related to huge investment in the LHC
 - An *e*⁻*p* collider operating at an energy frontier
 - *Guaranteed* to deepen the understanding of TeV-scale physics
- The LHeC needs the LHC proton/ion beams \Rightarrow synchronous pp and e^-p operation, as well as *HH* and $e^{-}H$, including deuterons.
- The earliest realistic operational period coincides with the LHC Run 5 period in 2032.

Review of the SMEFT

Standard Model Effective Field Theory:

- A model-independent extension to the Standard Model.
- Operators of dimensions higher than 4 built of the existing spectrum of SM.
- Wilson coefficients as effective couplings at UV scale Λ beyond accessible collider energies:

$$\mathscr{L}_{\rm SMEFT} = \mathscr{L}_{\rm SM}$$

- Focus on n = 6.
- Consider only SM-SMEFT interference in cross sections for consistency.

+
$$\sum_{n>4} \frac{1}{\Lambda^{n-4}} \sum_{k} C_{k}^{(n)} O_{k}^{(n)}$$

16 operators affecting DIS at leading order in the Warsaw basis [Misiak et al. 1008.4884]:

• Modifying *ffV* vertices in a nonuniversal manner: $O_{\boldsymbol{\omega}\boldsymbol{\ell}}^{(1)} = (\varphi^{\dagger}i \,\overleftrightarrow{D}_{\mu}\,\varphi)(\bar{\ell}\gamma^{\mu}\boldsymbol{\ell})$ $O^{(3)}_{\omega\ell} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \tau^{I} \varphi)(\bar{\ell} \gamma^{\mu} \tau^{I} \ell)$ $O_{\varphi e} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{e}\gamma^{\mu} e)$ $O_{\omega a}^{(1)} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{q} \gamma^{\mu} q)$ $O_{\omega a}^{(3)} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{q} \gamma^{\mu} \tau^{I} q)$ $O_{\varphi u} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{u} \gamma^{\mu} \tau^{I} u)$ $O_{\varphi d} = (\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi) (\bar{d} \gamma^{\mu} d)$

- Modifying *ffV* vertices in a universal manner:
- $O_{\varphi WB} = (\varphi$
- $O_{\varphi D} = (\varphi)^{T}$

 $\varphi^{\dagger}i \overleftrightarrow{D}_{\mu} \varphi =$ $\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\tau^{I}\varphi =$

$$(\sigma^{\dagger}\tau^{I}\varphi)W^{I}_{\mu
u}B^{\mu
u}$$

$$^{\dagger}D_{\mu} \varphi) * (\varphi^{\dagger}D^{\mu} \varphi)$$

$$= \varphi^{\dagger} i D_{\mu} \varphi + h.c.$$
$$= \varphi^{\dagger} i D_{\mu} \tau^{I} \varphi + h.c$$

• Inducing semi-leptonic 4fermion interaction:

$$\begin{split} O_{eu} &= (\bar{e}\gamma_{\mu}e)(\bar{u}\gamma^{\mu}u) \\ O_{ed} &= (\bar{e}\gamma_{\mu}e)(\bar{d}\gamma^{\mu}d) \\ O_{\ell q}^{(1)} &= (\bar{\ell}\gamma_{\mu}\ell)(\bar{q}\gamma^{\mu}q) \\ O_{\ell q}^{(3)} &= (\bar{\ell}\gamma_{\mu}\tau^{I}\ell)(\bar{q}\gamma^{\mu}\tau^{I}q) \\ O_{\ell u} &= (\bar{\ell}\gamma_{\mu}\ell)(\bar{u}\gamma^{\mu}u) \\ O_{\ell d} &= (\bar{\ell}\gamma_{\mu}\ell)(\bar{d}\gamma^{\mu}d) \\ O_{ed} &= (\bar{e}\gamma_{\mu}e)(\bar{q}\gamma^{\mu}q) \end{split}$$



Review of the DIS formalism



DIS cross section at LO

NC DIS in the process $\ell(k) + H(P) \rightarrow \ell'(k') + X$, where ℓ is e^{\pm} , *H* is *p* or *D*.

LO partonic process: $\ell(k) + q(p) \rightarrow \ell'(k') + q'(p')$



Possible gluon-initiated contact interaction: $\ell(k) + g(p) \rightarrow \ell'(k') + g'(p')$, but operators do not show up below dimension 8.



Parametrization of *ffV* and $\ell\ell qq$ vertex factors in V - A basis: where

• $V = \gamma, Z, \times$ in subscript

- V(A) means vector (axial) in superscript
- P, P' = V, A indicates structure of lepton and quark currents at the contact point (e.g. $C_{\times q}^{VA}$ for coupling of $\bar{\ell}\gamma_{\mu}\ell$ and $\bar{q}\gamma^{\mu}\gamma_{5}q$)
- all BSM effects are contained in $Q_{fV}^{V,A}$ for generalization to higher dimensions Propagator:



$$P_V = \frac{1}{Q_{_{18}}^2 + M_V^2}$$

Coupling strengths:

$$C_{\gamma} = -e = -\sqrt{4\pi\alpha}$$

$$C_{Z} = -g_{Z} = -\frac{e}{2c_{W}s_{W}} = -\sqrt{\sqrt{2}G_{F}M_{Z}^{2}}$$

$$C_{\times q}^{VV} = \frac{C_{eu/d} + (C_{\ell q}^{(1)} \mp C_{\ell q}^{(3)}) + C_{\ell u/d} + C_{qe}}{4\Lambda^{2}}$$

$$C_{\times q}^{VA} = \frac{C_{eu/d} - (C_{\ell q}^{(1)} \mp C_{\ell q}^{(3)}) + C_{\ell u/d} - C_{qe}}{4\Lambda^{2}}$$

$$C_{\times q}^{AV} = \frac{C_{eu/d} - (C_{\ell q}^{(1)} \mp C_{\ell q}^{(3)}) - C_{\ell u/d} + C_{qe}}{4\Lambda^{2}}$$

$$C_{\times q}^{AA} = \frac{C_{eu/d} + (C_{\ell q}^{(1)} \mp C_{\ell q}^{(3)}) - C_{\ell u/d} - C_{qe}}{4\Lambda^{2}}$$

Quantum numbers:

$$\begin{aligned} Q_{f\gamma}^{V} &= Q_{f} + \mathcal{O}(C_{k}^{2}) \\ Q_{f\gamma}^{A} &= 0 \\ Q_{fZ}^{V} &= g_{V}^{f} \left[1 + \frac{M_{Z}^{2}}{4\pi\alpha\Lambda^{2}} c_{V}^{f}(C_{k}^{V}, M_{Z}) \right] \\ Q_{fZ}^{V} &= g_{A}^{f} \left[1 + \frac{M_{Z}^{2}}{4\pi\alpha\Lambda^{2}} c_{A}^{f}(C_{k}^{A}, M_{Z}) \right] \end{aligned}$$

in the input basis $\{G_F, \alpha, M_Z\}$.

 $C_{k}^{V,A} \in \{C_{\varphi WB}, C_{\varphi D}, C_{\varphi \ell}^{(1)}, C_{\varphi \ell}^{(3)}, C_{\varphi e}, C_{\varphi q}^{(1)}, C_{\varphi q}^{(3)}, C_{\varphi u}, C_{\varphi d}\}$

Relative couplings and propagators:

$$\eta_V = \frac{C_V^2 P_V}{C_\gamma^2 P_\gamma}, \qquad \eta_{\times q}^{PP'} = \frac{C_{\times q}^{PP'}}{C_\gamma^2 P_\gamma}$$



SMEFT LO structure functions:

$$F_1^{\widetilde{V}}(x, Q^2) = \frac{1}{2} \sum_q \lambda_V^{\widetilde{V}} q(x, Q^2)$$
$$F_3^{\widetilde{V}}(x, Q^2) = \sum_q -\operatorname{sgn}(q) \lambda_A^{\widetilde{V}} q(x, Q^2)$$
$$F_L^{\widetilde{V}}(x, Q^2) = 0$$

$$g_{1}^{\widetilde{V}} = \frac{1}{2} \sum_{q} \lambda_{V}^{\widetilde{V}} \Delta q(x, Q^{2})$$
$$g_{5}^{\widetilde{V}}(x, Q^{2}) = \frac{1}{2} \sum_{q} \operatorname{sgn}(q) \lambda_{A}^{\widetilde{V}} \Delta q(x, Q^{2})$$
$$g_{L}^{\widetilde{V}}(x, Q^{2}) = 0$$

$\widetilde{V} = \gamma \gamma, \gamma Z, ZZ, \gamma \times (0), \gamma \times (1), Z \times (0), Z \times (1)$

NC DIS cross sections in structure-function formalism:



Reduced cross sections:

$$\frac{d^2 \sigma_{r,\text{NC}}^{\ell}}{dx \ dQ^2} = \left\{ \frac{4\pi\alpha^2}{xQ^4} [1 + (1 - y)^2] \right\}^{-1} \frac{d^2 \sigma_{\text{NC}}^{\ell}}{dx \ dQ^2}$$
$$\frac{d^2 \Delta \sigma_{r,\text{NC}}^{\ell}}{dx \ dQ^2} = \left\{ \frac{4\pi\alpha^2}{xQ^4} [1 + (1 - y)^2] \right\}^{-1} \frac{d^2 \Delta \sigma_{\text{NC}}^{\ell}}{dx \ dQ^2}$$

From here on, cross section means reduced cross section.

$$+ \operatorname{sgn}(\ell) [1 - (1 - y)^2] x F_3^{NC} + (1 - y)^2 F_L^{NC}$$



DIS cross section at NLO QCD

 $\ell + H \rightarrow \ell' + X$:



both SM and SMEFT structure functions. These corrections are well known [de Florian *et al.* 1210.7203].

Feynman diagrams describing NLO QCD corrections at parton level for the process

NLO QCD corrections take place only along the quark line \Rightarrow identical corrections to

SMEFT NLO structure functions:

$$F_{1}^{\widetilde{V}} = \frac{1}{2} \sum_{q} \lambda_{V}^{\widetilde{V}} \left[q + \frac{\alpha_{s}}{2\pi} \left(\widetilde{C}_{q_{1}} \otimes q + \widetilde{C}_{g_{1}} \otimes g \right) \right]$$
$$F_{3}^{\widetilde{V}} = \sum_{q} -\operatorname{sgn}(q) \lambda_{A}^{\widetilde{V}} \left[q + \frac{\alpha_{s}}{2\pi} \left(\widetilde{C}_{q_{3}} \otimes q + \widetilde{C}_{g_{3}} \otimes g \right) \right]$$
$$F_{L}^{\widetilde{V}} = x \sum_{q} \operatorname{sgn}(q) \lambda_{V}^{\widetilde{V}} \left[0 + \frac{\alpha_{s}}{2\pi} \left(\widetilde{C}_{q_{L}} \otimes q + \widetilde{C}_{g_{L}} \otimes g \right) \right]$$

$$g_{1}^{\widetilde{V}} = \frac{1}{2} \sum_{q} \lambda_{V}^{\widetilde{V}} \left[\Delta q + \frac{\alpha_{s}}{2\pi} \left(\widetilde{\Delta C}_{q_{1}} \otimes \Delta q + \widetilde{\Delta C}_{g_{1}} \otimes g \right) \right]$$
$$g_{5}^{\widetilde{V}} = \frac{1}{2} \sum_{q} \operatorname{sgn}(q) \lambda_{A}^{\widetilde{V}} \left[\Delta q + \frac{\alpha_{s}}{2\pi} \left(\widetilde{\Delta C}_{q_{3}} \otimes \Delta q + \widetilde{\Delta C}_{g_{3}} \otimes \Delta g \right) \right]$$
$$g_{L}^{\widetilde{V}} = \frac{1}{2} \sum_{q} \operatorname{sgn}(q) \lambda_{A}^{\widetilde{V}} \left[0 + \frac{\alpha_{s}}{2\pi} \left(\widetilde{\Delta C}_{q_{L}} \otimes \Delta q + \widetilde{\Delta C}_{g_{L}} \otimes \Delta g \right) \right]$$



PVDIS asymmetries to NLO QCD

Parity-violating DIS asymmetries in cross sections at the EIC:

• Lepton left-right asymmetries of unpolarized hadrons:

$$A_{\mathrm{PV}}^{\ell}$$
 =

• Hadron left-right asymmetries with unpolarized leptons:

where
$$\sigma^{\pm} = \frac{d^2 \sigma_{\text{NC}}^{\ell}}{dx \ dQ^2} \Big|_{\lambda_{\ell} = \pm |P_{\ell}|} \text{ and } (\Delta) \sigma^0$$

$$= \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-}$$



Generic form of cross sections:

For consistency, asymmetries must be linearized:

 $\sigma = \sigma_{\rm SM} + \sum_{k} C_k \, \delta \sigma_k$

 $A = A_{\rm SM} + \sum_{k} C_k \, \delta A_k$

Data analysis



Pseudodata sets

- sections of $e^{\pm}p$ collisions [Klein (2013)].
 - The entire error matrices are given.
- Preliminary EIC data sets used in [Boughezal et al. 2204.07557].

• Most recent publicly available official LHeC pseudodata sets for NC DIS cross

• We do not consider the 10-fold luminosity upgrade scenario at the EIC this time.

Data set label	Observable	Data set configuration
LHeC1	$\sigma_{ m NC}$	$60~{\rm GeV}\times 1000~{\rm GeV}~e^-p,~P_\ell$
LHeC2	$\sigma_{ m NC}$	$60~{\rm GeV}\times7000~{\rm GeV}~e^-p,~P_\ell$
LHeC3	$\sigma_{ m NC}$	$60~{\rm GeV}\times7000~{\rm GeV}~e^-p,~P_\ell$
LHeC4	$\sigma_{ m NC}$	$60~{\rm GeV}\times 7000~{\rm GeV}~e^+p,~P_\ell$
LHeC5	$\sigma_{ m NC}$	$60~{\rm GeV}\times7000~{\rm GeV}~e^-p,~P_\ell$
LHeC6	$\sigma_{ m NC}$	$60~{\rm GeV}\times7000~{\rm GeV}~e^-p,~P_\ell$
LHeC7	$\sigma_{ m NC}$	$60~{\rm GeV}\times7000~{\rm GeV}~e^+p,~P_\ell$
$(\Delta)D4$	$(\Delta)A_{\rm PV}$	10 GeV \times 137 GeV $e^-D,~ P_\ell$
$(\Delta)D5$	$(\Delta)A_{ m PV}$	18 GeV \times 137 GeV $e^-D,~ P_\ell$
$(\Delta)P4$	$(\Delta)A_{\rm PV}$	$10~{\rm GeV}\times 275~{\rm GeV}~e^-p,~ P_\ell $
(Δ) P5	$(\Delta)A_{ m PV}$	18 GeV \times 275 GeV $e^-p,~ P_\ell $

$$= 0, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

$$= -80\%, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

$$= +80\%, \ \mathcal{L} = 30 \ \text{fb}^{-1}$$

$$= +80\%, \ \mathcal{L} = 10 \ \text{fb}^{-1}$$

$$= -80\%, \ \mathcal{L} = 1000 \ \text{fb}^{-1}$$

$$= +80\%, \ \mathcal{L} = 300 \ \text{fb}^{-1}$$

$$= 0, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

$$= 80\%, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

$$= 80\%, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

$$= 80\%, \ \mathcal{L} = 100 \ \text{fb}^{-1}$$

Restrict ourselves to the bins with $x \leq 0.5$ $Q \ge 10 \text{ GeV}$ $0.1 \le y \le 0.9$ to avoid large uncertainties nonperturbative QCD and nuclear dynamics occurring at low *Q* and high *x*. Call them the good bins.



Kinematic coverage of the LHeC and EIC data sets: 1000 LHeC, $\sqrt{s} = 490 \text{ GeV}$ 500 LHeC, $\sqrt{s} = 1300 \text{ GeV}$ EIC, $\sqrt{s} = 70 \text{ GeV}$ Darker regions are *good* regions EIC, $\sqrt{s} = 140 \text{ GeV}$ 100 considered in our analysis. [GeV 50 \bigcirc 10 5 10^{-4} 0.001 0.010 0.100 10^{-5}

$$0.1 \le y = \frac{Q^2}{xs} \le 0.9$$

Lowest and highest CM energies are shown.

Anticipated uncertainties:

LHeC:

- statistical, $\delta\sigma_{\rm stat}$
- uncorrelated efficiency, $\delta\sigma_{\rm ueff}$
- full correlated systematics, $\delta\sigma_{\rm sys}$:
 - lepton energy scale, $\delta\sigma_{\rm len}$
 - lepton polar angle, $\delta\sigma_{\rm lpol}$
 - hadron energy scale, $\delta\sigma_{\rm hen}$
 - radiative corrections, $\delta\sigma_{\rm rad}$
 - photoproduction, $\delta\sigma_{\rm gam}$
 - global efficiency, $\delta\sigma_{\rm geff}$
 - luminosity, $\delta\sigma_{\rm lum}$, assumed 1 % rel. in $\sigma_{\rm NC}$

EIC:
• statistical,

$$\delta A_{\text{stat}} = \frac{1}{|P_{\ell}|} \frac{1}{\sqrt{N}}, \quad \delta \Delta A_{\text{stat}} = \frac{|P_{\ell}|}{|P_{H}|} \frac{1}{\sqrt{N}}$$

• uncorrelated systematics, $\delta \sigma_{\text{sys}}$, assumed 1 % rel. in
• fully correlated beam polarization, δA_{pol} ,
assumed 1 % for lepton beam, 2 % for hadron beam
rel. in A_{PV}

Assume $|P_{\ell}| = 80\%$ and $|P_{H}| = 70\%$.

Fully correlated PDF uncertainties, $\delta \sigma_{pdf}$ and δA_{pdf} , are considered, as well.





Size and rank of various uncertainty components going into the diagonal entries of the error matrix for the good bins:



- are the leading source of errors for unpolarized asymmetries at the EIC.
- among the lowest sources of errors at the EIC.
- to beam polarization, are a tiny part of total uncertainties at the EIC.

• **Stat** uncertainties are better controlled at the LHeC, constitute a minuscule part of total uncertainties. They

• Other uncorrelated uncertainties compete with systematics and PDF errors at the LHeC. Systematics are

• Systematics, correlated at the LHeC, forms the largest source of errors at the LHeC. Correlated errors, due

Numerical analysis

Numerical input:

- Input scheme: $\{G_F, \alpha, M_Z\}$
- Number of active quark flavors, $N_f = 5$
- UV cut-off scale: $\Lambda = 1$ TeV
- PDF sets: NNPDF3.1 NLO, NNPDFPOL1.1
- 2-loop running $\alpha_{s}(Q^{2})$

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Fitting procedure:

- Form the error matrix (experimental + PDF). 1.
- 2. Write down a χ^2 function.
- Minimize it and derive the covariance matrix of fitted parameters. 3.

Construction of the experimental error matrix:

• Uncorrelated errors:

$$\delta\sigma_{\text{unc},b} = \delta\sigma_{\text{stat},b} \oplus \delta\sigma_{\text{ueff},b}, \qquad \delta A_{\text{unc},b} = \delta A_{\text{stat},b} \oplus \delta A_{\text{sys},b} \qquad \text{at } b^{\text{th}} \text{ bin}$$

• Correlated errors:

$$\delta\sigma_{\text{cor},b} = \delta\sigma_{\text{len},b} \oplus \delta\sigma_{\text{lpol},b} \oplus \delta\sigma_{\text{hen},b} \oplus \delta\sigma_{\text{hen},$$

• Matrix elements:

$$E_{\exp,bb'} = \begin{cases} (\delta Q_{\text{unc}} \oplus \delta Q_{\text{cor}})_{bb}^2 \\ \rho_{bb'} \delta Q_{\text{cor},b} \delta Q_{\text{cor},b} \end{cases}$$

where we assume full correlations among bins, $\rho_{bb'} = 1$.

 $\delta\sigma_{\mathrm{rad},b} \oplus \delta\sigma_{\mathrm{gam},b} \oplus \delta\sigma_{\mathrm{geff},b} \oplus \delta\sigma_{\mathrm{cal},b} \oplus \delta\sigma_{\mathrm{lum},b}$ $a_{\mathrm{r},b} = \delta A_{\mathrm{pol},b}$

 $b_{bb'}, \quad b = b'$ $b_{bb'}, \quad b \neq b'$ $Q = \sigma, A$: observable

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Construction of the PDF error matrix:

$$E_{\text{pdf},bb'} = \frac{1}{N_{\text{pdf}}} \sum_{m=1}^{N_{\text{pdf}}} \left(\frac{1}{m}\right)$$

the b^{th} bin and $N_{\text{pdf}} = 100$ is the number of replica PDF members.

 $(Q_{m,b} - Q_{0,b})(Q_{m,b'} - Q_{0,b'})$

where $Q_{0(m),b}$ is the observable evaluated at the central (m^{th}) member of the PDF set at

Total error matrix:

E = E

 χ^2 test statistic for the e^{th} pseudoexperiment:

$$\chi_{e}^{2} = \sum_{b,b'=1}^{N_{\text{bin}}} (Q_{b}^{\text{SMEFT}} - Q_{e,b}) E_{bb'}^{-1} (Q_{b'}^{\text{SMEFT}} - Q_{e,b'})$$

Pseudoexperimental observable:

$$Q_{e,b} = Q_b^{\text{SM}} + r_{e,b} \ \delta Q_{\text{unc},b} + r'_e \ \delta Q_{\text{cor},b}, \qquad r_{e,b}, r'_e \sim \mathcal{N}(0,1)$$

$$E_{\rm exp} + E_{\rm pdf}$$

SMEET fit results





- others make up for it.

- e^+p collisions (LHeC₄ and LHeC₇) yield the optimal configuration for $C_{\ell u}$ and $C_{\ell d}$.
- e^+p collisions with unpolarized positrons (LHeC₇) serve as the optimal configuration for C_{qe} .
- No single LHeC run seems to be the *best* configuration to constrain all semi-leptonic 4-fermion Wilson coefficients.

• LHeC imposes significantly stronger bounds than EIC with few exceptions. When one run yields weaker bounds, the

• Low-luminosity e^-p collisions with RH electrons (LHeC3 and LHeC6) provide the optimal configuration for C_{eu} and C_{ed} . • High-luminosity e^-p collisions with LH electrons (LHeC2 and LHeC5) is the optimal configuration for $C_{\ell q}^{(1)}$ and $C_{\ell q}^{(3)}$.





- A large subset of LHeC runs can go beyond 5 TeV.
- Only few LHeC runs can exceed 10 TeV at 95% CL.

• EIC can probe UV scales up to 2 TeV, and does so with its strongest data set, P4.

Strongest EIC and two strongest LHeC:

- The LHeC runs are significantly more constraining than the EIC.
- These data sets exhibit distinct correlations, complementary to each other.
- Even the two *strongest* LHeC runs can yield nearly orthogonal correlations.

Strongest EIC and two strongest LHeC:

- LHC NC DY is 8 TeV 20 fb⁻¹, not
 13 TeV and HL; adapted from
 [Boughezal *et al.* 2104.03979].
- When LHC NC DY is blind to a part of the parameter space, EIC and LHeC can resolve these blind spots, imposing strong bounds.
- LHeC fits can lead to correlations parallel to LHC NC DY, whereas EIC yields a new correlation axis.

Strongest EIC and two strongest LHeC:

- LHC NC DY is 8 TeV 20 fb⁻¹, not
 13 TeVand HL; adapted from
 [Boughezal *et al.* 2104.03979].
- LHC NC DY is again blind to this part of the parameter space.
- There is a slight degeneracy at the LHeC, as well.
- LHeC and EIC may yield correlations in the same directions, though in a different direction than LHC NC DY.

Data set label	Observable	Data set configuration
LHeC1	$\sigma_{ m NC}$	$60~{ m GeV} imes 1000~{ m GeV}~e^-p,~P_\ell=0,~\mathcal{L}=$
LHeC2	$\sigma_{ m NC}$	60 GeV × 7000 GeV e^-p , $P_{\ell} = -80\%$,
LHeC3	$\sigma_{ m NC}$	60 GeV × 7000 GeV e^-p , $P_{\ell} = +80\%$,
LHeC4	$\sigma_{ m NC}$	60 GeV × 7000 GeV e^+p , $P_{\ell} = +80\%$,
LHeC5	$\sigma_{ m NC}$	60 GeV × 7000 GeV e^-p , $P_{\ell} = -80\%$,
LHeC6	$\sigma_{ m NC}$	60 GeV × 7000 GeV e^-p , $P_{\ell} = +80\%$,
LHeC7	$\sigma_{ m NC}$	$60~{ m GeV} imes 7000~{ m GeV}~e^+p,~P_\ell=0,~\mathcal{L}=$

- Compare LHeC1 to LHeC2 to understand effects of beam polarization.
- lepton species.

=
$$100 \text{ fb}^{-1}$$

 $\mathcal{L} = 100 \text{ fb}^{-1}$
 $\mathcal{L} = 30 \text{ fb}^{-1}$
 $\mathcal{L} = 10 \text{ fb}^{-1}$
 $\mathcal{L} = 1000 \text{ fb}^{-1}$
 $\mathcal{L} = 300 \text{ fb}^{-1}$
= 100 fb^{-1}

Which parameter is the most important?

- Luminosity?
- Beam polarization?
- Lepton species?

• Compare LHeC₂ to LHeC₅ and LHeC₃ to LHeC₆ to check importance of luminosity.

Compare LHeC1 to LHeC7 and LHeC3 to LHeC4 to investigate consequences of

 Converting from low- to high-luminosity e^-p collisions can improve the bounds in a noticeable manner; however, the improvements are not sharp.

LHeC2: 60 GeV × 7000 GeV e^-p , $P_{\ell} = -80\%$, $\mathcal{L} = 100 \text{ fb}^{-1}$ LHeC5: 60 GeV × 7000 GeV e^-p , $P_{\ell} = -80\%$, $\mathcal{L} = 1000 \text{ fb}^{-1}$ LHeC3: 60 GeV × 7000 GeV e^{-p} , $P_{\ell} = +80\%$, $\mathscr{L} = 30 \text{ fb}^{-1}$ LHeC6: 60 GeV × 7000 GeV e^{-p} , $P_{\ell} = +80\%$, $\mathscr{L} = 300 \text{ fb}^{-1}$

- Converting from low- to high-luminosity e^-p collisions can improve the bounds in a noticeable manner; however, the improvements are not sharp.
- Shifting from unpolarized to LH electrons can lead to more distinguishable improvements than increasing luminosity.

LHeC1: 60 GeV × 1000 GeV e^{-p} , $P_{\ell} = 0\%$, $\mathscr{L} = 100 \text{ fb}^{-1}$ LHeC2: 60 GeV × 7000 GeV e^-p , $P_{\ell} = -80\%$, $\mathcal{L} = 100 \text{ fb}^{-1}$

- Converting from low- to high-luminosity
 e⁻p collisions can improve the bounds in a noticeable manner; however, the improvements are not sharp.
- Shifting from unpolarized to LH electrons can lead to more distinguishable improvements than increasing luminosity.
- The most drastic improvements on the bounds occur when we change lepton species from electrons to
 positrons. LHeC1: 60 GeV × 1000 GeV e⁻p, P_e = 0%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = 0%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = 0%, LHeC1: 60 GeV × 7000 GeV e⁻p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%, LHeC1: 60 GeV × 7000 GeV e⁺p, P_e = + 80%

Joint LHeC run

- Join all 7 LHeC runs with <u>nontrivial correlations</u>.
- correlated between runs:
 - global efficiency, calorimetry noise, luminosity, and PDF errors
 - background events fluctuates without any correlations.

• We assume only a subset of correlated uncertainties of individual data sets are

• lepton energy scale and polar angle, hadron energy scale, radiative corrections,

• photoproduction is excluded because said background consists of different events for each run; therefore, if we run an experiment multiple times, number of

χ^2 function for the n^{th} run: $\chi_n^2 = (\text{LHeC}n)^{-1}$

χ^2 function for the joint run: $\chi^2 = (LHeC)$

where

$$J_{nn'} = J_{\exp,nn'} + J_{pdf,nn'}$$
$$J_{\exp,nn',bb'} = \rho_{nn',bb'} \widetilde{\delta\sigma}_{n,\operatorname{cor},b} \widetilde{\delta\sigma}_{n',\operatorname{cor},b'}, \quad \rho_{nn',bb'} = 1$$
$$J_{pdf,nn',bb'} = \frac{1}{N_{pdf}} \sum_{m=1}^{N_{pdf}} (\sigma_{n,m,b} - \sigma_{n,0,b}) (\sigma_{n',m,b'} - \sigma_{n',0,b'})$$

with $\delta \sigma_{n, \text{cor}, b}$ the same as for a single run defined before but with photoproduction errors removed.

(n)
$$(E_n)^{-1}$$
 (LHeCn)
C1 ... LHeC7) $\begin{pmatrix} E_1 & \cdots & J_{17} \\ \vdots & \ddots & \vdots \\ J_{71} & \cdots & E_7 \end{pmatrix}^{-1} \begin{pmatrix} LHeC \\ \vdots \\ LHeC \end{pmatrix}$

- LHeC set for any Wilson coefficient.
- Nonetheless, it is comparable to the strongest LHeC data set.

Strongest EIC, strongest and weakest LHeC, and the joint LHeC for each Wilson coefficient: C_k at 95% CL, $\Lambda = 1$ TeV, 7d fit

• Allowed bound from the joint run is significantly more restricting than the *weakest*

Strongest EIC, strongest and weakest LHeC, and the joint LHeC for each Wilson coefficient:

- UV scales present a clearer picture of comparison.
- In a joint run, the LHeC can probe UV scales beyond 15 TeV.

• Compared to the strongest LHeC run, UV scales that can be probed get deeper by 20 to 30%.

Two *strongest* LHeC sets and the joint fit for double Wilson coefficient:

- The joint fit seems to offer bounds just comparable to the *strongest* LHeC run in 1*d* parameter subspaces. Its real power emerges in 2*d* parameter subspaces.

• Constraints are highly restricting and correlations are different than those of the two strongest LHeC sets.

Two *strongest* LHeC sets and the joint fit for double Wilson coefficients:

- The joint fit still offers considerably stronger bounds.

• It may not always yield remarkably distinct correlations than the individual runs.

Flat-direction analysis

SMEFT part of unpolarized hadronic cross section:

$$\frac{d^2 \sigma_{\ell H}(\lambda_{\ell})}{dx \ dQ^2} \supset \sum_{q} \frac{1}{2} \left[\frac{d^2 \sigma_{\ell q}^{\gamma \times +Z \times}(\lambda_{\ell}, \lambda_H = 1)}{dx \ dQ^2} + \frac{d^2 \sigma_{\ell q}^{\gamma \times +Z \times}(\lambda_{\ell}, \lambda_H = -1)}{dx \ dQ^2} \right] f_{q/H}$$

Set SMEFT contributions equal to zero to investigate blind spots. Two structures, 1 and $(1 - y)^2$, and two types of quarks, u_i and $d_i \Rightarrow$ four equations \Rightarrow number of free Wilson coefficients becomes 7 - 4 = 3.

We focus on four different bases spanned by free Wilson coefficients:

- Basis 1: $\{C_{\ell q}^{(1)}, C_{\ell q}^{(3)}, C_{qe}\} \Rightarrow \text{all LH quarks}$
- Basis 2: { C_{eu}, C_{ed}, C_{qe} } \Rightarrow all RH leptons
- Basis 3: $\{C_{\ell a}^{(1)}, C_{\ell a}^{(3)}, C_{\ell u}\} \Rightarrow$ all LH leptons with a focus on the up-quark channel
- Basis 4: $\{C_{\ell a}^{(1)}, C_{\ell a}^{(3)}, C_{\ell d}\} \Rightarrow$ all LH leptons with a focus on the down-quark channel

Examples to flat-direction relations:

$$\text{Basis 1:} (C_{\ell q}^{(1)}, C_{\ell q}^{(3)}, C_{q e}) \begin{cases} C_{eu} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}}{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} - C_{\ell q}^{(3)}) \\ C_{\ell u} = \frac{P_{\ell} + 1}{P_{\ell} - 1} \frac{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}}{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}} C_{q e} \\ C_{ed} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} + C_{\ell q}^{(3)}) \\ C_{\ell d} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} + C_{\ell q}^{(3)}) \\ C_{\ell d} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} + C_{\ell q}^{(3)}) \\ C_{\ell d} = \frac{P_{\ell} - 1}{P_{\ell} - 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} C_{q e} \end{cases}$$

Flat directions defined by these relations are only approximate due to the energydependent eta factors:

They become exact only in the limit $Q^2/$

 $\eta_{\gamma}\eta_{Z}$

$$\eta_{\gamma}\eta_{Z} = \frac{G_{F}M_{Z}^{2}}{2\sqrt{2}\pi\alpha} \frac{Q^{2}}{Q^{2} + M_{Z}^{2}}$$

the limit $Q^{2}/M_{Z}^{2} \to \infty$. Thus, we assume
 $\eta_{\gamma}\eta_{Z} \approx \frac{G_{F}M_{Z}^{2}}{2\sqrt{2}\pi\alpha}$

Examples to flat-direction relations:

$$\text{Basis 1:}(C_{\ell q}^{(1)}, C_{\ell q}^{(3)}, C_{q e}) \begin{cases} C_{eu} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}}{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} - C_{\ell q}^{(3)}) \\ C_{\ell u} = \frac{P_{\ell} + 1}{P_{\ell} - 1} \frac{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}}{Q_{u} - g_{e}^{e} g_{u}^{u} \eta_{\gamma} \eta_{Z}} C_{q e} \\ C_{ed} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} + C_{\ell q}^{(3)}) \\ C_{\ell d} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} (C_{\ell q}^{(1)} + C_{\ell q}^{(3)}) \\ C_{\ell d} = \frac{P_{\ell} - 1}{P_{\ell} + 1} \frac{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}}{Q_{d} - g_{u}^{d} g_{e}^{e} \eta_{\gamma} \eta_{Z}} C_{q e} \end{cases}$$

Moreover, the LHeC runs have only very specific polarization values:

- Case 1: Unpolarized leptons, $P_{\ell} = 0$: LHeC1 and 7
- Case 2: RH/LH electrons/positrons, $P_{\ell} = \pm 80\%$: LHeC2, 4, and 5
- Case 3: LH/RH electrons/positrons, $P_{\ell} = \mp 80\%$: LHeC3 and 6 Shown data sets are in each case are enforced to exhibit flat directions. We want to see if the EIC can resolve these blind spots; therefore, we now include other EIC sets in our comparison, as well. ⁵⁵

We indeed observe weaker constraints or diminished UV probes in the expected cases of flat directions. The good news is, other LHeC runs seem promising in resolving these blind spots; in fact, LHeC3 and LHeC6 appear highly enthusiast to in most cases.

However, the four *strongest* EIC data sets can barely compete in resolving degeneracies with LHeC runs that survive flat-direction conditions.

Extended parameter space

- Turn on Wilson coefficients in the ffV sector now.
- Purpose is to see if the LHeC can resolve the degeneracies observed the EWPO fits.
- 9 operators shifting the *ffV* vertices \Rightarrow 16 fitted parameters now.

95% CL bounds in single-parameter fits at $\Lambda = 1$ TeV

[1909.02000]

	Joint LHeC	Dawson's	
$C_{\varphi WB}$	[-0.020, 0.020]	[-0.0088, 0.0013]	[
$C_{\varphi D}$	[-0.030, 0.030]	[-0.025, 0.0019]	
$C^{(3)}_{\varphi\ell}$	[-0.067, 0.067]	[-0.012, 0.0029]	
$\mathrm{C}^{(1)}_{arphi\ell}$	[-0.067, 0.067]	[-0.0043, 0.012]	
$C_{\varphi e}$	[-0.11, 0.11]	[-0.013, 0.0094]	
$C^{(3)}_{\varphi q}$	[-0.080, 0.080]	[-0.011, 0.014]	
$\mathrm{C}^{(1)}_{arphi \mathrm{q}}$	[-0.16, 0.16]	[-0.027, 0.043]	
$C_{\varphi d}$	[-0.22, 0.22]	[-0.16, 0.060]	
$C_{\varphi u}$	[-0.091, 0.091]	[-0.072, 0.091]	

Comments on actual fits:

16*d* fit to joint LHeC runs 9*d* global fit to Z and Wpole observables

[2012.02779]

34*d* global fit to EW, diboson, Higgs, and top data

EWPO fits better constrain the relevant Wilson coefficients in the ffV sector in single-parameter fits.

Shown bounds are for single Wilson coefficients activated one at a time.

Comparison of double-parameter fits:

Comments:

• Shown are the non-marginalized ellipses.

(Only 2 Wilson coefficients are activated at a time.)

• EWPO fits are adapted from [Mimasu et al. 2012.02779].

Resolution of flat directions observed in EWPO fits:

Comments:

- EWPO fits are adapted from [Mimasu *et al.* 2012.02779].

• Shown are the non-marginalized ellipses. (Only 2 Wilson coefficients are activated at a time.) 60

Coda

Conclusion

- We have studied the BSM potential of the EIC and LHeC to NLO QCD within the modelindependent framework of the SMEFT.
- space to include the SMEFT ffV corrections, all at dimension 6.
- We have found that
 - joint fit;
 - lead to distinct correlations, indicating complementarity;

• We have focused on the semi-leptonic 4-fermion operators first and then extended our parameter

• the EIC can probe UV scales ~ 2 TeV and the LHeC > 10 TeV and even > 15 TeV with a

• the bounds from the EIC may barely compete with the ones from the LHeC; nevertheless, they

• both the EIC and LHeC can strongly resolve degeneracies observed in the LHC NC Drell-Yan fits;

• one LHeC fit may suffer from blind spots itself, but another LHeC fit or even the EIC resolves it;

• the LHeC seems promising in resolving flat directions observed in the ffV sector in the EWPO fits.

Outlook

- Promotion of the EIC data sets to include SMEFT ffV corrections (in progress)
- Upgrade of both EIC and LHeC to include dimension-8 SMEFT operators
 - 54 operators but not all independent
 - Vertex factors already extracted
 - A possible LanHEP code to more syste channel them into FeynArts directly
- EW corrections to study HERA data
- Switching from Mathematica to a faster la for cross sections

e SMEFT *ffV* corrections (in progress) le dimension-8 SMEFT operators

• A possible LanHEP code to more systematically obtain Feynman rules, allowing one to

• Switching from Mathematica to a faster language and writing a comprehensive package